

Package ‘JlfdR’

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Type Package

Title JlfdR: Controlling the Joint Local False Discovery Rate in Joint Analysis of Summary Statistics from Multiple GWASs

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Description

The most powerful summary-statistics-based joint analysis method when controlling the false discovery rate at a certain level. We can use it to analyze multiple GWASs with the same phenotype together to discover associated genetic variants with higher power.

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Depends R (>= 2.10), mvtnorm

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R topics documented:

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JlfdR-package	<i>JlfdR: Controlling the Joint Local False Discovery Rate in Joint Analysis of Summary Statistics from Multiple GWASs</i>
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Description

The most powerful summary-statistics-based joint analysis method when controlling the false discovery rate at a certain level. We can use it to analyze multiple GWASs with the same phenotype together to discover associated genetic variants with higher power.

Details

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License: GPL-3

In genome-wide association studies (GWASs) of common diseases/traits, we often analyze multiple GWASs with the same phenotype together to discover associated genetic variants with higher power. Since it is difficult to access data with detailed individual measurements, summary-statistics-based meta-analysis methods have become popular to jointly analyze data sets from multiple GWASs.

Here we implement a novel summary-statistics-based joint analysis method based on controlling the joint local false discovery rate (JlfdR). This method is the most powerful summary-statistics-based joint analysis method when controlling the false discovery rate (Fdr) at a certain level. Details about the method can be seen in our reference paper below.

The principal component of JlfdR package is `FdrControl2`. Also we implement a Fdr controlling method `BayesFdr` for single-study analysis.

1. To jointly analyze summary statistics from multiple GWASs, we need to obtain the z-values of each genotyped SNPs in all studies. We have put example summary statistics of two studies (`SmryStats1` and `SmryStats2`) in our package. You can use `data(SmryStats1)` and `data(SmryStats2)` to load the example data. You can also obtain the ground-truth parameters (allele frequencies, odds ratios) of the example data using `data(Param1)` and `data(Param2)`

2. You can use `FdrControl2` to jointly analyze summary statistics from two studies.

```
FdrControl2(z1, z2, K=2, q=0.05, beta0=length(z1)/5, plot=T, output=T, dir=output)
```

Details about the function can be seen using [help\(FdrControl2\)](#).

3. To analyze summary statistics from single study with controlling Fdr, `BayesFdr` can be used.

```
BayesFdr(z, q, K = 2, beta0 = length(z)/5)
```

Details about the function can be seen using [help\(BayesFdr\)](#)

Author(s)

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References

Jiang, W. and Yu, W. *Controlling the joint local false discovery rate is more powerful than meta-analysis methods in joint analysis of summary statistics from multiple genome-wide association studies*. Submitted.

See Also

[FdrControl2](#), [BayesFdr](#)

Examples

```

q<-5e-5                #Fdr Threshold

##Load data
data(SmryStats1)       #Example of summary statistics in 1st study
data(SmryStats2)       #Example of summary statistics in 2nd study

z1<-SmryStats1$Z       #Z values in 1st study
z2<-SmryStats1$Z       #Z values in 2nd study

##### Jlfdr-based method #####
FdrResult<-FdrControl2(z1,z2, K=2, beta0=length(z1)/5, q=q,dir=.)
rejectedIdx<-FdrResult$rejected #The indexes of the rejected null hypotheses

```

BayesFdr-functions *Functions to control Fdr in single-study analysis*

Description

BayesFdr is a (Bayesian) Fdr controlling method used in single-study analysis. snpEM is a built-in function to infer the parameters in the one-dimensional Gaussian Mixture Model. calBayesFdr is a built-in function to calculate the Fdr after given parameters in the Gaussian Mixture Model.

Usage

```

BayesFdr(z, q, K = 2, beta0 = length(z)/5)

snpEM(z, K=2, maxIter=1000, tol=1e-4, beta0=length(z)/5, info=TRUE)

calBayesFdr(t, Pi1, sigma2)

```

Arguments

z	The vector containing z values of all SNPs.
q	The Fdr controlling level.
K	The components number of the z values in associated SNPs.
beta0	The penalty term for pi0. We add Dirichlet(beta0, 0) prior to proportions (pi0, Pi1).
maxIter	The maximum number of iterations.
tol	The relative error tolerance.
info	A logical number indicating whether the results should be printed out.
t	The critical value for z-values.
Pi1	The vector including the proportion of each associated component.
sigma2	The vector including the variance of standardized effect sizes in each associated component.

Details

These functions are the implementation of controlling the Fdr in single-study analysis. Here we assume the z-values follow the (K+1)-component Gaussian Mixture Model:

$$Z \sim \pi_0 N(0,1) + \sum_{k=1}^K \pi_k N(0, 1 + \sigma_k^2).$$

snpEM is a built-in function to infer the parameters in the one-dimensional Gaussian Mixture Model using EM-algorithm.

calBayesFdr is a built-in function to calculate the Fdr after given parameters in the Gaussian Mixture Model.

BayesFdr is a Fdr controlling method used in single-study analysis. snpEM and calBayesFdr are called in BayesFdr.

Value

BayesFdr returns the critical value and the indexes of the rejected null hypotheses. The returned value is a LIST:

thld The determined critical value in terms of z-value.
idx The indexes of the rejected null hypotheses.

snpEM returns the inferred parameters and the iteration status. The returned value is a LIST:

pi0 The inferred proportion of true null hypotheses.
Pi1 The vector including the inferred proportion of each associated component.
sigma2 The vector including the inferred variance of standardized effect sizes in each associated component.
h0 The vector including the probability of being true null hypothesis for each SNP.
h A K-vector list. Each vector includes the probability of being component k (1 ≤ k ≤ K) for each SNP.
iter The iteration number.
Qval The expected negative log-likelihood.

calBayesFdr returns the Fdr value for a given threshold t.

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References

Jiang, W. and Yu, W. *Controlling the joint local false discovery rate is more powerful than meta-analysis methods in joint analysis of summary statistics from multiple genome-wide association studies*. Submitted.

See Also

[Jlfdr](#), [FdrControl2](#)

Examples

```

q<-5e-5                #Fdr Threshold

##Load data
data(SmryStats1)      #Example of summary statistics in 1st study

z1<-SmryStats1$Z      #Z values in 1st study

####Bayes Fdr Control###
FdrResult<-BayesFdr(z1, q=q, K=2, beta0=length(z1)/5)
rejectedIdx<-FdrResult$idx #The indexes of the rejected null hypotheses

```

Jlfr-functions	<i>Functions to control Fdr in joint analysis of multiple GWASs via Jlfr-based method</i>
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Description

FdrControl2 is a novel summary-statistics-based joint analysis method to infer which SNPs have associations with traits. The method is based on controlling the joint local false discovery rate (Jlfr). snpEM2 is a built-in function to infer the parameters in the Gaussian Mixture Model. calJlfr2 is a built-in function to calculate the Jlfr of each SNP after given parameters in the Gaussian Mixture Model.

Usage

```

FdrControl2(z1, z2, K = 2, q = 0.05, beta0 = length(z1)/5, plot = T,
  output = T, dir = "output")

snpEM2(z1, z2, K=2, maxIter=1000, tol=1e-4, beta0=length(z1)/5, info=TRUE)

calJlfr2(z1, z2, Pi1, Sigma)

```

Arguments

z1	The vector containing z values of all SNPs from Study 1.
z2	The vector containing z values of all SNPs from Study 2.
K	The components number of the z values in associated SNPs.
q	The Fdr controlling level.
beta0	The penalty term for π_0 . We add Dirichlet(beta0, 0) prior to proportions (π_0 , π_1).
plot	A logical number indicating whether to plot the discovered associations in the z-value plane.
output, info	A logical number indicating whether the results should be printed out.
dir	The directory to save the results when output=T
maxIter	The maximum number of iterations.
tol	The relative error tolerance.
Pi1	The vector including the proportion of each associated component.
Sigma	A K-objects list. Each object is the covariance matrix of standardized effect size vector in the corresponding associated component.

Details

These functions are the implementation of Jlfr-based method to control the Fdr in joint analysis of multiple GWASs. Here we assume the z-value vector follow the (K+1)-component Gaussian Mixture Model:

$$Z \sim \pi_0 N(0, I) + \sum_{k=1}^K \pi_k N(0, I + \Sigma_k).$$

snpEM2 is a built-in function to infer the parameters in the Gaussian Mixture Model using EM-algorithm.

calJlfr2 is a built-in function to calculate the Jlfr of each SNP after given parameters in the Gaussian Mixture Model.

FdrControl2 is based on controlling the joint local false discovery rate (Jlfr) in the joint analysis of multiple GWASs. snpEM2 and calJlfr2 are called in FdrControl2.

Value

FdrControl2 returns the following LIST:

Pi1	The vector including the inferred proportion of each associated component.
Sigma	A K-objects list. Each object is the inferred covariance matrix of standardized effect size vector in the corresponding associated component.
rejected	The indexes of the rejected null hypotheses.
JlfrThld	The determined threshold for Jlfr.
Jlfr	The vector including the calculated Jlfr value for each SNP.

snpEM2 returns the inferred parameters and the iteration status. The returned value is a LIST:

pi0	The inferred proportion of true null hypotheses.
Pi1	The vector including the inferred proportion of each associated component.
Sigma	A K-objects list. Each object is the inferred covariance matrix of standardized effect size vector in the corresponding associated component.
h0	The vector including the probability of being true null hypothesis for each SNP.
h	A K-vector list. Each vector includes the probability of being component k ($1 \leq k \leq K$) for each SNP.
iter	The iteration number.
Qval	The expected negative log-likelihood.

calJlfr2 returns the calculated Jlfr value for each SNP.

Author(s)

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References

Jiang, W. and Yu, W. *Controlling the joint local false discovery rate is more powerful than meta-analysis methods in joint analysis of summary statistics from multiple genome-wide association studies*. Submitted.

See Also[Jlfd](#), [BayesFdr](#)**Examples**

```
q<-5e-5                #Fdr Threshold

##Load data
data(SmryStats1)       #Example of summary statistics in 1st study
data(SmryStats2)       #Example of summary statistics in 2nd study

z1<-SmryStats1$Z       #Z values in 1st study
z2<-SmryStats2$Z       #Z values in 2nd study

##### Jlfd-based method #####
FdrResult<-FdrControl2(z1,z2, K=2, beta0=length(z1)/5, q=q,dir=.)
rejectedIdx<-FdrResult$rejected #The indexes of the rejected null hypotheses
```

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